# Genomewide Prediction Accuracy within 969 Maize Biparental Populations

Lian Lian, Amy Jacobson, Shengqiang Zhong, and Rex Bernardo\*

#### **ABSTRACT**

In genomewide selection, the expected correlation between predicted and true genotypic values  $(r_{MG})$  has been previously derived as a function of the training population size (N), heritability  $(h^2)$ , and effective number of chromosome segments  $(M_{\rm s})$  affecting the trait. Our objectives were to determine: (i) the mean and variability of  $r_{\rm MG}$  in 969 biparental maize (Zea mays L.) breeding populations for seven traits, (ii) if  $r_{\rm MG}$  can be predicted in advance, and (iii) how N, h2, and number of markers ( $N_{\rm M}$ ) affect  $r_{\rm MG}$ . We modified a previous equation for expected  $r_{\rm MG}$  to account for linkage disequilibrium (r2) between a marker and a quantitative trait locus (QTL). Across the 969 populations, the mean and range (in parentheses) of observed  $r_{\rm MG}$  was 0.45 (-0.59, 1.03) for grain yield, 0.59 (-0.34, 0.96) for moisture, 0.55 (-0.24, 1.10) for test weight, 0.49 (-0.22,1.04) for stalk lodging, 0.41 (-0.30, 0.93) for root lodging, 0.47 (-0.45, 0.97) for plant height, and 0.42 (-0.43, 0.94) for ear height. The observed  $r_{\rm MG}$  values were centered around the expected  $r_{\rm MG}$  when  $r^2$  was accounted for, but the observed  $r_{MG}$  had a large spread around the expected  $r_{\rm MG}$ . The  $r^2(Nh^2)^{1/2}$  had the strongest association with observed  $r_{\rm MG}$ . When  $r^2(Nh^2)^{1/2}$  exceeded 8, the proportion of  $r_{\rm MG}$  equal to or larger than 0.50 reached 90% among all the populationtrait combinations. We conclude it is difficult to predict  $r_{\rm MG}$  in advance, but that rules of thumb based on  $r^2(Nh^2)^{1/2}$  can help achieve a high  $r_{MG}$ .

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**Abbreviations:** DH, doubled haploid;  $E(r_{MG})$ , expected prediction accuracy;  $h^2$ , heritability;  $M_e$ , effective number of chromosome segments; N, population size;  $N_M$ , number of markers; QTL, quantitative trait locus;  $r^2$ , linkage disequilibrium;  $r_{MG}$ , correlation between predicted and true genotypic values; RR-BLUP, ridge regression-best linear unbiased prediction; SNP, single nucleotide polymorphism;  $V_G$ , genetic variance;  $V_B$ , nongenetic variance.

Maize breeding typically involves crossing two inbred parents, developing inbred progeny from the biparental cross, and selecting the best new inbreds on the basis of testcross performance (Hallauer, 1990). Traditionally, selection for complex traits has been done by field evaluation of testcrosses in multiple environments. Genomewide selection (or genomic selection) (Meuwissen et al., 2001) allows the prediction of genotypic values of individuals for complex traits on the basis of marker information. In genomewide selection, marker effects are estimated from a training population, which has been genotyped and phenotyped. Genotypic values of individuals in a test population, which has been genotyped but not phenotyped, are then predicted from the marker effects estimated from the training population.

Different breeding schemes for genomewide selection have been proposed and studied in maize and in other species (Bernardo, 2009; Bernardo and Yu, 2007; Heffner et al., 2010; Riedelsheimer et al., 2012, 2013; Windhausen et al., 2012). Regardless of the breeding scheme, the  $r_{\rm MG}$  must be high enough for

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genomewide selection to be time and cost effective. The expected prediction accuracy  $[E(r_{\rm MG})]$  has been previously derived as a function of N,  $h^2$ , and  $M_{\rm e}$  affecting the trait (Daetwyler et al., 2008):

$$E(r_{MG}) = \left[ Nh^2 / \left( Nh^2 + M_e \right) \right]^{1/2}$$
 [1]

The  $M_{\rm e}$  pertains to the idealized concept of having independent chromosome segments, with each segment containing a QTL-marker pair and with all the QTL having additive, equal effects (Daetwyler et al., 2008; Goddard, 2009). When the genome is saturated by markers,  $M_{\rm e}$  is generally calculated on the basis of the effective population size and the genome size (Goddard, 2009; Lorenz, 2013; Meuwissen and Goddard, 2010). The  $M_{\rm e}$  can also be calculated by the eigenvalues of the marker correlation matrix, according to the same approach for calculating the effective number of independent tests in association mapping when the markers are highly correlated (Li and Ji, 2005).

Before they commit time and resources to genomewide selection, breeders want to know whether or not  $r_{\rm MG}$  will be high enough in a cross. Previous empirical studies on the correspondence between observed and predicted  $r_{\rm MG}$  have been few and were limited by the number of populations studied. In five maize biparental crosses, the observed  $r_{\rm MG}$  agreed well with the  $r_{\rm MG}$  expected from Eq. [1] (Riedelsheimer et al., 2013). In four crosses in maize, barley (*Hordeum vulgare* L.) and *Arabidopsis thaliana* (L.) Heynh, the observed  $r_{\rm MG}$  generally agreed with E( $r_{\rm MG}$ ) but uncertainty in  $M_{\rm e}$  made the comparisons difficult (Combs and Bernardo, 2013a).

The current study utilizes phenotypic and marker data from 969 biparental maize populations in the Monsanto breeding program. The data in this study therefore represent the genetic backgrounds, traits,  $h^2$ , population sizes, and extent of testing in a commercial breeding program. As such, the data can give a realistic indication of the  $r_{\rm MG}$  for different traits in maize and of the correspondence between the observed and expected  $r_{MG}$  when genomewide selection is routinely practiced on a wide scale. To avoid any confounding effects of a difference in the genetic constitution of the training population and test population (Daetwyler et al., 2008), we analyzed each of the 969 biparental crosses individually. Our objectives were to determine: (i) the mean and variability of  $r_{MG}$  in maize biparental populations, (ii) if  $r_{\rm MG}$  can be reliably predicted in advance; and (iii) the how  $r_{\rm MG}$  is affected by traits,  $h^2$ , N, and  $N_{\rm M}$  in biparental populations.

# MATERIALS AND METHODS Phenotypic and Marker Data

The 969 maize populations comprised two maize heterotic groups, with 485 biparental crosses in Group 1 and 484 crosses in Group 2. The number of lines in each cross ranged from

35 to 356 and had a mean of 156. The lines in each cross were derived from the following generations (number of crosses in parentheses):  $F_2$  (707),  $BC_1$  (186),  $BC_1F_2$  (47), doubled haploid (DH) from  $F_1$  (17), and DH from  $F_2$  (12). For the  $F_2$ ,  $BC_1$ , and  $BC_1F_2$  populations, plants grown from 10 to 15 selfed seeds derived from each individual plant were testcrossed to an inbred tester from the opposite heterotic group. For DH populations, each DH line was crossed to an inbred tester.

The populations were evaluated for the following traits: grain yield (Mg ha<sup>-1</sup>), moisture (g H<sub>2</sub>O kg<sup>-1</sup>), test weight (kg hl<sup>-1</sup>), stalk lodging (%), root lodging (%), plant height (cm), and ear height (cm). Each experiment was conducted in 2 to 15 locations (usually 6–8 locations) during a single year (2000–2008). Phenotypic data were available as the testcross mean of each line at each location. Not all traits were measured in all locations and in all populations (Table 1). To help ensure that the lodging traits were adequately expressed within a location, only those locations with a mean stalk lodging of at least 5% or a mean root lodging of at least 5% were retained for these two traits, and a population was retained for these two traits only if data were available for more than one location.

The number of polymorphic single nucleotide polymorphism (SNP) markers used to genotype the lines in each population ranged from 31 to 119 and had a mean of 70. The parents of the 969 populations were genotyped with 2911 SNP markers. The lines within each cross were genotyped with 31 to 119 (mean of 70) SNP markers that were polymorphic between the two parents and that were a subset of the 2911 SNP markers used for genotyping all the parents. When the set of markers (31 to 119 SNP loci) used for each population did not have data for some lines, the missing marker data were imputed with fastPHASE (Scheet and Stephens, 2006); imputation with the full set of 2911 parental markers was not done. A segregating SNP locus was disregarded if the parents were monomorphic, if the minor allele frequency was <0.10, or if more than half of the data points were missing. Populations with < 30 markers were removed from analysis.

#### Heritability

Within each cross, testcross genetic (V<sub>G</sub>) and nongenetic (V<sub>R</sub>) variance components were calculated for each trait by restricted maximum likelihood via the "lmer" function in the "lme4" package (Bates et al., 2013). Because the data were entry means within each location, the genotype by environment interaction variance and within-location error variance were confounded in V<sub>R</sub>. A likelihood ratio test was used to test the significance of the estimates of testcross genetic variance. The p-value from the likelihood ratio test was divided by 2.0 to approximate an F-test of the null hypothesis (Holland et al., 2003). Genetic variance estimates with a p-value > 0.05 were considered not significant and the corresponding population-trait combination was discarded. The data for each biparental cross were not completely balanced because some individuals were not evaluated at a few of the locations in each experiment. As such, the  $h^2$  was estimated on an ad hoc basis as  $h^2 = V_G/(V_G + V_R/l)$ , where l was the harmonic mean of the number of locations (Holland et al., 2003).

# Observed $r_{\rm MG}$

Genomewide marker effects were obtained by ridge-regression best linear unbiased prediction (RR-BLUP) as described by

Table 1. Mean and range of entry-mean heritability ( $h^2$ ) and prediction accuracy ( $r_{\rm MP}$  and  $r_{\rm MG}$ ) for different traits in 3371 population–trait combinations in 969 maize biparental crosses.

		<u> </u>		$r_{MP}$		r <sub>MG</sub>			
Trait	Populations	Mean	Range	Mean	Range	Mean	Range	50% quantiles	Standard deviation
Yield	840	0.46	(0.17, 0.92)	0.30	(-0.34, 0.89)	0.45a <sup>†</sup>	(-0.59, 1.03)	(0.32, 0.59)	0.23
Moisture	943	0.66	(0.24, 0.91)	0.48	(-0.18, 0.81)	0.59c	(-0.34, 0.96)	(0.53, 0.71)	0.19
Test weight	894	0.56	(0.18, 0.92)	0.41	(-0.21, 0.78)	0.55b	(-0.24, 1.10)	(0.46, 0.69)	0.20
Stalk lodging	68	0.33	(0.19, 0.67)	0.28	(-0.13, 0.55)	0.49ab	(-0.22, 1.04)	(0.40, 0.64)	0.24
Root lodging	38	0.32	(0.19, 0.53)	0.23	(-0.17, 0.47)	0.4a	(-0.30, 0.93)	(0.21, 0.67)	0.30
Plant height	369	0.39	(0.18, 0.82)	0.29	(-0.27, 0.69)	0.47a	(-0.45, 0.97)	(0.33, 0.62)	0.24
Ear height	219	0.33	(0.17, 0.63)	0.24	(-0.21, 0.59)	0.42a	(-0.43, 0.94)	(0.27, 0.61)	0.25

 $<sup>^{\</sup>dagger}$   $r_{MG}$  values followed by the same letter were not significantly different according to a Tukey HSD test (P = 0.05).

Meuwissen et al. (2001) and by Bernardo and Yu (2007). Suppose the phenotypic data comprised  $N_{\rm T}$  records, each record being the mean performance of an individual in one of the  $N_{\rm L}$  locations. The linear model was as  ${\bf y}={\bf X}{\bf b}+{\bf Z}{\bf m}+{\bf e},$  where  ${\bf y}$  was an  $N_{\rm T}\times 1$  vector of phenotypic records,  ${\bf b}$  was an  $N_{\rm L}\times 1$  vector of fixed effects of locations,  ${\bf m}$  was an  $N_{\rm M}\times 1$  vector of random effects of the markers,  ${\bf e}$  was an  $N_{\rm T}\times 1$  vector of residuals,  ${\bf X}$  was an  $N_{\rm T}\times N_{\rm L}$  incidence matrix that related  ${\bf y}$  to  ${\bf b}$ , and  ${\bf Z}$  was in  $N_{\rm T}\times N_{\rm M}$  incidence matrix (with values of 1 and -1 for each of the two homozygotes and 0 for the heterozygote) that related  ${\bf y}$  to  ${\bf m}$ . The variance of marker effects was  $V_{\rm G}/N_{\rm M}$  (Meuwissen et al., 2001).

The  $r_{\text{MP}}$  for each trait within each population was estimated by a delete-one method (Kohavi, 1995). Suppose a population had  $N_p = 100$  lines that had been phenotyped. The first line was assumed untested and its performance was predicted from genomewide marker effects estimated from RR-BLUP analysis of lines 2 to 100. The second line was then assumed untested and its performance was predicted from RR-BLUP analysis of the remaining  $N = N_p - 1$  lines. In the end, the correlation between the predicted genotypic value and the mean phenotypic value of the  $N_p$  lines was calculated and was denoted by  $r_{\rm MP}$ . The value of  $r_{\rm MG}$  was calculated as  $r_{\rm MP}$  divided by the square root of  $h^2$  (Dekkers, 2007). For each  $r_{MP}$ , we calculated the test statistic T =  $[r_{MP}(N_P - 2)^{1/2}]/(1 - r_{MP}^2)$ ], which follows a  $t_{\rm N-2}$  distribution (Bobko, 2001). Significance tests for  $r_{\rm MP}$  (via T) were done through a t test. Given that significance tests for genetic variances had been previously done, we assumed for simplicity that  $r_{MG}$  was significantly different from zero if  $r_{MP}$ was significantly different from zero.

# Expected $r_{\text{MG}}$ with Incomplete Linkage Disequilibrium

Equation [1] was derived with the following four assumptions (Daetwyler et al., 2008). First, the marker effects were derived from simple linear regression rather than from RR-BLUP, which we used in this study. Second, each marker–QTL pair was assumed independent of other marker–QTL pairs. Third, the different marker–QTL pairs (which were to be accounted for by  $M_{\rm e}$ ) were assumed to have equal variances. Fourth, each marker–QTL pair was assumed in complete linkage disequilibrium. We modified Eq. [1] to retain the first three assumptions by Daetwyler et al. (2008) but to relax the last assumption. By accounting for incomplete linkage disequilibrium between a

marker and QTL, we obtained the following  $E(r_{MG})$  with  $r^2 < 1$  (Appendix 1 in Supplemental Material):

$$E(r_{MG_{-}r^{2}}) = r^{2} [Nh^{2} / (r^{2}Nh^{2} + M_{e})]^{1/2}$$
 [2]

In Eq. [2], we used  $r^2=r^2$ , the latter being the mean squared correlation between a marker and QTL when the QTL is assumed to be at the midpoint of the two markers. The midpoint, in turn, is the mean QTL position assuming a uniform distribution between two markers. The  $r^2$  can be calculated as the square root of the observed squared correlation between two marker genotypes. We found that  $r^2_{\text{MM}/2}=\sqrt[3]{r^2_{\text{MM}}}$  for BC<sub>1</sub>, F<sub>2</sub>, and DH populations but not for BC<sub>1</sub>F<sub>2</sub> populations (Appendix 2 in Supplemental Material). The  $E(r_{\text{MG}\_r2})$  values were therefore not calculated for the 47 BC<sub>1</sub>F<sub>2</sub> populations. For all the following analyses, we used  $r^2=r^2$ . Although the assumption of complete linkage between a marker and a QTL was relaxed, Eq. [2] assumed that the distance between a QTL and a marker is constant for all marker–QTL pairs.

For each population, the  $M_{\rm e}$  values were calculated by eigenvalues of the linkage disequilibrium matrix among the SNP markers in each population (Li and Ji, 2005). This matrix was obtained by computing all pairwise squared correlations for markers on each individual chromosome. Eigenvalue decomposition was done with the "eigen" function in R (R Development Core Team, 2012). Given the known values of N and the estimated values of  $h^2$ ,  $r^2$ , and  $M_{\rm e}$ , the expected  $r_{\rm MG}$  was calculated according to both Eq. [1] and [2].

Because of the uncertainty in the proper form of  $M_{\rm e}$ , we also back-calculated  $M_{\rm e}$  by equating the observed  $r_{\rm MG}$  with the expected  $r_{\rm MG}$  from Eq. [1] and [2] and solving for  $M_{\rm e}$ . This procedure was performed for all population—trait combinations (excluding BC<sub>1</sub>F<sub>2</sub>) where the observed  $r_{\rm MG}$  was between 0.1 and 1.

## Factors Affecting $r_{\rm MG}$

We evaluated the relative importance of the following factors in terms of the variance in  $r_{\rm MG}$  explained by each factor: trait,  $h^2$ , training population size (N being equal to  $N_{\rm P}-1$ ),  $N_{\rm M}$ , heterotic group, and generation type. Given their prominence in Eq. [1] or [2], we evaluated the variance explained by  $(Nh^2)^{1/2}$  and  $r^2(Nh^2)^{1/2}$ . For each trait, we also obtained the correlation coefficient between the observed  $r_{\rm MG}$  and the following:  $(Nh^2)^{1/2}$ ,  $r^2(Nh^2)^{1/2}$ ,  $E(r_{\rm MG})$  from Eq. [1], and  $E(r_{\rm MG}, r_2)$  from Eq. [2].

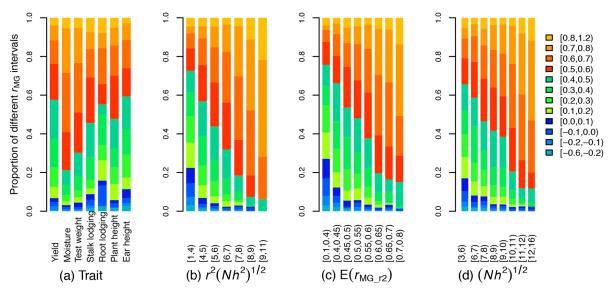


Figure 1. Distribution of observed prediction accuracy  $(r_{MG})$  in biparental maize populations for: (a) different traits for 3371 population-trait combinations, (b) different  $r^2(Nh^2)^{1/2}$ , (c) different expected  $r_{MG}$  from Eq. [2]  $[E(r_{MG-r2})]$ ; and (d) different  $(Nh^2)^{1/2}$ . Data in b, c, and d were for 3217 population-trait combinations for which  $BC_1F_2$  populations were excluded. N=1 training population size, N=1 training size, N=1 training population size, N=1 training size, N=

To further investigate the effect of N on  $r_{\rm MG}$ , 1533 population—trait combinations with rounded (to the nearest tens digit) values of  $N_{\rm P}=180$  were selected. For each population—trait combination, a random subset of  $N_{\rm P}=61,91,121,$  and 151 lines were obtained as a new population and the  $r_{\rm MP}$  within the new population was estimated by a delete–one method as described before, so that N was 60, 90, 120, and 150. For each population—trait combination, only one random sample for the new population was obtained because the results were to be averaged over 1533 populations. The value of h used for calculating  $r_{\rm MG}$  (Dekkers, 2007) was that obtained with the largest  $N_{\rm P}$ .

Similarly, to investigate the effect of  $N_{\rm M}$  on  $r_{\rm MG}$ , 45 population—trait combinations whose  $N_{\rm M}$  values were larger than 100 were selected. Markers were thinned to 2/3 of their original density by keeping only the first two markers out of every three consecutive markers. Likewise, markers were thinned to 1/3 of their original density by keeping only the first marker out of every three consecutive markers. The  $r_{\rm MP}$  within the new population was estimated by a delete-one method as described before.

The effect of  $h^2$  on  $r_{\rm MG}$  was further studied for the population—trait combinations with rounded  $N_{\rm p}=180$ . Heritability values were subdivided into several intervals and the mean  $r_{\rm MG}$  in each interval was calculated. For each trait, if the number of populations in an interval was < 20, the mean  $r_{\rm MG}$  values for that trait were not calculated for that interval and the data were not shown for that trait in the interval. Because we only had a limited number of observations that met the above criteria for stalk lodging and root lodging, this analysis was not done for these two traits.

Likewise, the effect of  $(Nh^2)^{1/2}$  and  $r^2(Nh^2)^{1/2}$  on  $r_{\rm MG}$  was examined by subdividing  $(Nh^2)^{1/2}$  and  $r^2(Nh^2)^{1/2}$  into different intervals. For each trait, if the number of populations in an interval was < 20, the mean  $r_{\rm MG}$  values for that trait were not calculated for that interval and the data were not shown for that

trait in that interval. This analysis was not done for stalk lodging and root lodging and not for BC<sub>1</sub>F<sub>2</sub> populations.

To assess their distribution,  $r_{\rm MG}$  values were divided into different intervals and the proportion of  $r_{\rm MG}$  in each interval was plotted against different traits for all population—trait combinations and plotted against different  $(Nh^2)^{1/2}$ , different  $r^2(Nh^2)^{1/2}$ , and different values of  $E(r_{\rm MG\_r2})$  for population—trait combinations excluding  $BC_1F_2$ .

#### **RESULTS AND DISCUSSION**

# Mean and Variability of Observed $r_{\rm MG}$

Out of 3371 population—trait combinations, 2919 (87%) had an  $r_{\rm MG}$  that was significantly different from zero (P=0.05). The mean  $r_{\rm MG}$  was 0.52 and the individual  $r_{\rm MG}$  values ranged from –0.59 to 1.10 (Table 1). The mean  $r_{\rm MP}$  was 0.37 and the individual  $r_{\rm MP}$  values ranged from –0.34 to 0.89 (Table 1). The  $r_{\rm MG}$  was estimated indirectly as  $r_{\rm MP}/h$  (Dekkers, 2007), and the  $r_{\rm MG}$  values that exceeded 1.0 were due to sampling variation in both  $r_{\rm MP}$  and  $h^2$ . Only 11 of the 3371 population—trait combinations (0.3%) had an  $r_{\rm MG}$  that was negative and significantly different from zero (P=0.05).

The mean, range, and standard deviation of  $r_{\rm MG}$  values differed among the seven traits. The mean  $r_{\rm MG}$  was highest for moisture and lowest for root lodging (Table 1). Conversely, the standard deviation of  $r_{\rm MG}$  was smallest for moisture and largest for root lodging. For grain yield, which was the most important trait (Bernardo, 1991), the mean  $r_{\rm MG}$  across 840 populations was 0.45 (-0.59, 1.03) and around 40% of the populations had an  $r_{\rm MG}$  equal to or larger than 0.50 (Fig. 1a). The middle 50% of  $r_{\rm MG}$  values for grain yield ranged from 0.32 to 0.59. For moisture, which was the second most important trait (Bernardo,

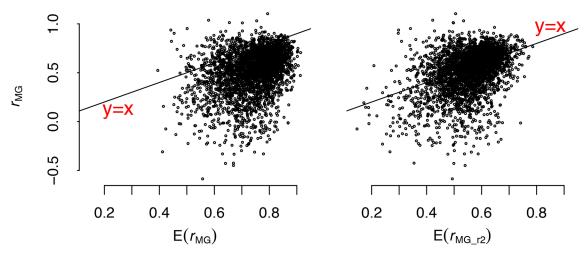


Figure 2. Observed prediction accuracy ( $r_{MG}$ ) versus expected prediction accuracy from Eq. [1] [E( $r_{MG}$ )] and Eq. [2] [E( $r_{MG\_r2}$ )] for 3217 population–trait combinations (BC<sub>1</sub>F<sub>2</sub> populations excluded) in 969 maize biparental crosses.

1991), the mean  $r_{\rm MG}$  (range in parentheses) across 943 populations was 0.59 (-0.34, 0.96) and around 80% of the populations had an  $r_{\rm MG} \ge 0.50$ . The middle 50% of  $r_{\rm MG}$  values for moisture ranged from 0.53 to 0.71.

Among the seven traits studied, stalk lodging and root lodging are the two traits that are generally considered by maize breeders as the least consistent in their expression. However, the mean  $r_{\rm MG}$  for stalk lodging (0.49) and the mean  $r_{\rm MG}$  for root lodging (0.41) were not significantly different from the mean  $r_{\rm MG}$  for grain yield (0.45). Overall, the results from this 969-population study indicated that the mean  $r_{\rm MG}$  for yield and other agronomic traits in maize biparental crosses is in the 0.40 to 0.60 range.

# Expected $r_{\rm MG}$

There were 3217 population—trait combinations after removing the BC<sub>1</sub>F<sub>2</sub> populations, for which  $r^2$  cannot be calculated as the square root of the observed squared correlation between two markers. Whereas the mean  $r_{\rm MG}$  across all the 3217 population—trait combinations was 0.52, the mean expected  $r_{\rm MG}$  according to Eq. [1] [mean E( $r_{\rm MG}$ )] was 0.74. Equation [1] (Daetwyler et al., 2008), which assumes perfect linkage between a marker and QTL, therefore grossly overestimated  $r_{\rm MG}$  (by 0.74 – 0.52 = 0.22). The mean expected  $r_{\rm MG}$  according to Eq. [2] [mean E( $r_{\rm MG\_r2}$ )] was 0.56. Equation [2], which accounts for imperfect linkage between a marker and QTL, still overestimated  $r_{\rm MG}$ , but the amount of upward bias (0.56 – 0.52 = 0.04) was much less than with Eq. [1] from Daetwyler et al. (2008).

The mean  $r_{\rm MG}$  was closer to  $E(r_{\rm MG\_r2})$  for some traits than for others. These  $r_{\rm MG}-E(r_{\rm MG\_r2})$  deviations were 0.092 for grain yield, 0.004 for moisture, 0.008 for test weight, 0.021 for stalk lodging, 0.102 for root lodging, 0.058 for plant height, and 0.080 for ear height. Across all traits, the spread of  $r_{\rm MG}$  about the mean and about  $E(r_{\rm MG\_r2})$  was large (Fig. 2).

Pooled across all traits, the correlation between  $r_{MG}$  and  $E(r_{MG-r})$  was 0.40, whereas the correlation between

Table 2. Correlation between prediction accuracy  $(r_{\rm MG})$  and different combinations of factors that affect  $r_{\rm MG}$  for different traits in 3217 population–trait combinations (BC<sub>1</sub>F<sub>2</sub> populations excluded) in 969 maize biparental crosses.

Trait	Popula- tions	r <sup>2</sup> (Nh <sup>2</sup> ) <sup>1/2</sup>	E(r <sub>MG_r2</sub> )	(Nh²) <sup>1/2</sup>	E(r <sub>MG</sub> )
Yield	799	0.30*b†B‡	0.32*aB	0.21*aA	0.21* bA
Moisture	898	0.45*cB	0.44*bB	0.36*bC	0.32*cdA
Test weight	850	0.43*cB	0.43*bB	0.34*bcA	0.34*dA
Stalk lodging	64	-0.02aA	-0.06cdA	-0.02adA	-0.06aeA
Root lodging	37	-0.04aA	-0.17dA	-0.20dA	-0.32eA
Plant height	358	0.23*abA	0.21*aA	0.22*aA	0.19*abA
Ear height	211	0.20*abA	0.19*acA	0.20*acA	0.18*abcA
All	3217	0.41	0.40	0.36	0.33

<sup>\*</sup> Significant at the 0.05 probability level.

 $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG})$  was 0.33. The correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG_{-}r2})$  was significantly different (P=0.05) from the correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG})$  for grain yield, moisture, and test weight, but was not significantly different for stalk lodging, root lodging, plant height, and ear height (Table 2). The correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG_{-}r2})$  ranged from -0.17 for root lodging to 0.44 for moisture (Table 2). The correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG})$  ranged from -0.32 for root lodging to 0.34 for test weight. The correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG_{-}r2})$  was lower for grain yield than for moisture and test weight. Likewise, the correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG})$  was lower for grain yield than for moisture and test weight.

The usefulness of Eq. [1] and of Eq. [2] for predicting  $r_{\text{MG}}$  therefore differed among traits. Overall, the results for observed  $r_{\text{MG}}$  and expected  $r_{\text{MG}}$  indicated that although

 $<sup>^\</sup>dagger$  Within columns (across different traits), correlation values followed by the same lowercase letter were not significantly different according to Fisher z-transformations (P=0.05; Bobko, 2001).

 $<sup>^{\</sup>ddagger}$  Within rows (across different factor combinations), correlation values followed by the same uppercase letter were not significantly different (P=0.05). Significance tests were done by transforming the correlations to Fisher's z and considering that the correlations were nonindependent because they shared the same common variable  $r_{\rm MG}$  (Bobko, 2001).

the mean  $r_{\rm MG}$  across many different populations and traits can be predicted fairly well by Eq. [2], the  $r_{\rm MG}$  for any given trait in any given population cannot be predicted reliably with either Eq. [1] from Daetwyler et al. (2008) or with Eq. [2], which we derived.

Equation [2] had the following parameters:  $r^2$ , N,  $h^2$ , and  $M_e$ . As shown later, the observed  $r_{MG}$  was correlated with  $r^2(Nh^2)^{1/2}$ , which was the numerator of Eq. [2]. This result suggested that the failure to accurately predict  $r_{MG}$ was mainly due to the failure of  $M_{e}$  to adequately mimic the assumptions of equal and additive effects of marker-QTL pairs. We suggest four other reasons for the inability to predict  $r_{MG}$ : (i) while we accounted for imperfect linkage disequilibrium between a QTL and a marker in Eq. [2], this imperfect linkage disequilibrium itself led to not all QTL effects being captured and, consequently, to missing  $h^2$  (Makowsky et al., 2011; Manolio et al., 2009) in the model; (ii) the linear additive model did not capture all of the genetic variance due to epistasis not being modeled; (iii) sampling error in the estimates of  $r_{MP}$  and  $h^2$ , which were used in estimating  $r_{MG}$ , contributed to a lower observed correlation between  $r_{MG}$  and  $E(r_{MG-r_2})$ ; and (iv) uncertainty remains regarding the proper method to calculate  $M_a$ .

Previous studies have calculated  $M_e$  as  $2N_eL$ , where  $N_e$  is the effective population size and L is the size of the genome in Morgans (Daetwyler et al., 2008). In a maize biparental population in which all individuals are in theory derived from  $N_e = 1$  F<sub>1</sub> plant, the  $M_e$  is approximately 30 when  $M_e$  is calculated as  $2N_eL$ . An  $M_e$  of 30 always overestimated  $r_{\rm MG}$  in the populations used in this study.

The  $M_{e}$  values we used, which were calculated according to Li and Ji (2005), ranged from 28 to 119 and had a mean of 59 in 3034 population–trait combinations (BC<sub>1</sub>F<sub>2</sub> populations excluded and  $r_{MG}$  between 0.1 and 1). Because  $N_{\rm M}$  was relatively low, these  $M_{\rm e}$  values did not differ much from the actual  $N_{\rm M}$ , which ranged from 31 to 119 and had a mean of 70. When  $M_e$  was back-calculated by equating the observed  $r_{MG}$  to  $E(r_{MG})$  from Eq. [1] and solving for  $M_{\rm e}$ , the estimated values of  $M_{\rm e}$  ranged from 242 to 525. These  $M_{\epsilon}$  values back-calculated from Eq. [1] were much larger than the  $M_e$  calculated according to the Li and Ji (2005) method, larger than the actual  $N_{\rm M}$ , and larger than the value of 30 obtained as  $2N_cL$  (Table 2). When  $M_c$  was back-calculated by equating the observed  $r_{MG}$  to  $E(r_{MG\_r2})$ from Eq. [2], the estimated values of  $M_e$  ranged from 29 to 110. These  $M_{\epsilon}$  values back-calculated from Eq. [2] were of similar magnitude to the  $M_e$  calculated according to the Li and Ji (2005) method as well as to  $N_{\rm M}$  (Table 2).

Furthermore, the back-calculated  $M_{\rm e}$  values differed among the traits (Table 3). Among the three traits with the most data, grain yield had the largest back-calculated  $M_{\rm e}$  values whereas moisture and test weight had similar back-calculated  $M_{\rm e}$  values. This result was consistent with the perceived complexity of the traits, with grain yield

Table 3. Effective number of chromosome segments ( $M_{\rm e}$ ) back-calculated from Eq. [1] and [2] for seven different traits in 3034 population-trait combinations (prediction accuracy between 0.1 and 1; BC<sub>1</sub>F<sub>2</sub> populations excluded) from 969 maize biparental populations.

Trait	Popula- tions	Mean N <sub>M</sub> †	M <sub>e</sub> from Li and Ji (2005)	Mean M <sub>e</sub> from Eq. [1]	Mean M <sub>e</sub> from Eq. [2]
Yield	742	70	59	468a <sup>‡</sup>	82c
Moisture	869	70	59	275b	29a
Test weight	811	70	59	283b	38ab
Stalk lodging	57	68	57	242ab	40ac
Root lodging	31	69	57	525ab	110ac
Plant height	338	72	60	434a	86c
Ear height	186	73	61	374ab	72bc

 $<sup>^{\</sup>dagger}N_{\mathrm{M}}$ , number of markers used in genomewide prediction in each biparental population

conceivably being controlled by more QTL compared with moisture and test weight. In contrast,  $M_{\rm e}$  calculated according to the Li and Ji (2005) method or as  $2N_{\rm e}L$  leads to the same  $M_{\rm e}$  across all traits. Overall, these results suggest that other methods need to be developed for calculating  $M_{\rm e}$ .

# Association between $r_{\rm MG}$ and Different Factor Combinations

Whereas the best way to estimate  $M_{\rm e}$  is unclear, N in Eq. [1] and [2] were known and  $h^2$  and  $r^2$  were estimated in this study with well-established procedures. We found that  $r^2(Nh^2)^{1/2}$  was most strongly associated with  $r_{\rm MG}$ . When only the intercept and a specific factor or a combination of factors was fitted, the variance in  $r_{\rm MG}$  explained by the regression model was as follows:  $r^2(Nh^2)^{1/2}$ , 17.1%;  $(Nh^2)^{1/2}$ , 12.9%; trait, 8.4%;  $h^2$ , 7.8%; N, 4.4%; generation type, 0.4%; heterotic group, 0.0%; and  $N_{\rm M}$ , 0.0%. The importance of  $r^2(Nh^2)^{1/2}$  in influencing  $r_{\rm MG}$  was in accordance with  $r^2(Nh^2)^{1/2}$  being the numerator of Eq. [2]. When  $r^2(Nh^2)^{1/2}$  exceeded 8, more than 90% of the  $r_{\rm MG}$  values were  $\geq$  0.50 (Fig. 1b).

The correlation between  $r_{\rm MG}$  and  $r^2(Nh^2)^{1/2}$  was not significantly different (P=0.05) from the correlation between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG\_r2})$  for each trait (Table 2). In other words,  $r_{\rm MG}$  was as strongly associated with  $r^2(Nh^2)^{1/2}$  as it was with  ${\rm E}(r_{\rm MG\_r2})$ . The correlations of the different factors with  $r_{\rm MG}$  were higher for grain yield, moisture, and test weight than for stalk lodging, root lodging, plant height, and ear height. Across all the traits, the correlation between  $r_{\rm MG}$  and  $r^2(Nh^2)^{1/2}$  was 0.41, between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG\_r2})$  was 0.40, between  $r_{\rm MG}$  and  $(Nh^2)^{1/2}$  was 0.36, and between  $r_{\rm MG}$  and  ${\rm E}(r_{\rm MG})$  was 0.33. Overall, these results indicated that  ${\rm E}(r_{\rm MG\_r2})$  and  $r^2(Nh^2)^{1/2}$  were the best predictors of  $r_{\rm MG}$ , and that breeders could manipulate  $r^2(Nh^2)^{1/2}$  to get a high  $r_{\rm MG}$  (Fig. 1b).

The mean  $r_{MG}$  varied among traits when  $r^2(Nh^2)^{1/2}$  or  $(Nh^2)^{1/2}$  was kept constant (Fig. 3b, c). Grain yield

<sup>&</sup>lt;sup>‡</sup> Within columns, values followed by the same letter were not significantly different according to a Tukey HSD test (*P* = 0.05).

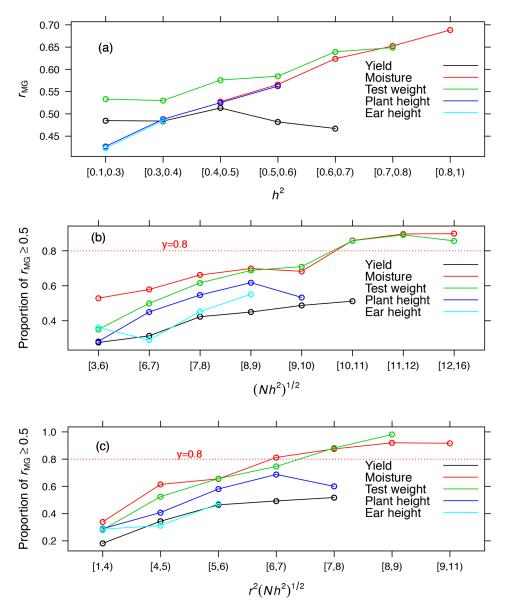


Figure 3. (a) Mean prediction accuracy ( $r_{\rm MG}$ ) in different intervals of entry-mean heritability ( $h^2$ ) for five different traits in 1430 population—trait combinations with rounded training population sizes of  $N_{\rm P}=180$ ; (b) proportion of  $r_{\rm MG}$  equal to or larger than 0.50 in different intervals of ( $Nh^2$ )<sup>1/2</sup> for five different traits in 3062 population—trait combinations (BC<sub>1</sub>F<sub>2</sub> populations excluded); and (c) proportion of  $r_{\rm MG}$  equal to or larger than 0.50 in different intervals of  $r^2(Nh^2)^{1/2}$  for five different traits in 3073 population—trait combinations (BC<sub>1</sub>F<sub>2</sub> populations excluded). N=10 training population size, N=11 training population size, N=12 training population size, N=13 the mean linkage disequilibrium between a marker and quantitative trait locus (QTL) when the QTL was assumed to be at the midpoint of the two markers. For all the above plots, population—trait combinations in an interval with <20 data points were excluded.

tended to have a lower  $r_{\rm MG}$  compared with moisture, test weight, and plant height at a fixed  $r^2(Nh^2)^{1/2}$  or  $(Nh^2)^{1/2}$ . For grain yield and plant height, the proportion of  $r_{\rm MG}$  equal to or larger than 0.50 did not change much beyond  $r^2(Nh^2)^{1/2}=6$  and plateaued at around 50% for grain yield and 60 to 70% for plant height. The proportion of  $r_{\rm MG}$  equal to or larger than 0.50 increased to above 80% for moisture and test weight when  $r^2(Nh^2)^{1/2}$  exceeded 7.

## Association between $r_{\rm MG}$ and Individual Factors

As has been found in previous studies (Combs and Bernardo, 2013a; Crossa et al., 2013; Lorenzana and Bernardo, 2009), increases in the individual factors N,  $h^2$ , and  $N_{\rm M}$  generally led

to increases in  $r_{\rm MG}$ , particularly when it was possible to keep other factors constant. There were 1533 population—trait combinations with the rounded number of lines equal to 180. The mean  $r_{\rm MG}$  for different training population sizes was 0.41 with N=60, 0.46 with N=90, 0.51 with N=120, 0.54 with N=150, and 0.55 with rounded N=180. These mean  $r_{\rm MG}$  values were significantly different from each other (P=0.05), except for  $r_{\rm MG}$  with N=150 vs. rounded N=180.

When the rounded N was fixed at 180,  $r_{\rm MG}$  increased as  $h^2$  increased for grain yield, moisture, test weight, plant height, and ear height (Fig. 3a). However, the  $r_{\rm MG}$  for yield did not change much beyond  $h^2 = 0.40$ . In contrast, the  $r_{\rm MG}$  for moisture and plant height kept increasing as  $h^2$  increased.

As mentioned above,  $N_{\rm M}$  explained none of the total variance in  $r_{\rm MG}$  when other factors were not kept constant. When all other factors were kept constant and the markers were thinned to 2/3 and 1/3 of their original number, the mean  $r_{\rm MG}$  was 0.45 when 1/3 of the markers were used ( $N_{\rm M}=36$ ), 0.49 when 2/3 of the markers were used ( $N_{\rm M}=72$ ), and 0.50 when all of the markers were used ( $N_{\rm M}=107$ ). These mean  $r_{\rm MG}$  values across different marker densities were not significantly different from each other (P=0.05). In the above subset of populations, the mean  $r^2$  value between adjacent markers was 0.16 when 1/3 of the markers were used, 0.41 when 2/3 of the markers were used, and 0.52 when all of the markers were used.

A minimum  $r^2$  of 0.20 between adjacent markers has been suggested for genomewide selection (Hayes et al., 2009). The mean  $r^2$  values between adjacent markers was 0.46 across the 969 biparental maize populations used in this study. The  $r^2$  values are typically high in biparental populations because large chromosome segments are passed intact from the inbred parents to the progeny (Smith et al., 2008). The high  $r^2$  between adjacent markers in this study was probably due to having only one meiosis in the development of lines from the F<sub>2</sub> or BC<sub>1</sub> populations, which constituted 92% of the 969 biparental crosses. These high  $r^2$  values suggest that with maize biparental crosses, a fairly small number of SNP markers ( $N_{\rm M} = 70$ -120) is largely sufficient for genomewide selection. This agrees with a previous study that found that  $r_{MG}$  was at or near maximum when the mean distance between markers was around 25 cM in a DH maize population (Lorenzana and Bernardo, 2009). On the basis of a linkage map of about 1750 cM (Senior et al., 1996), a 25-cM spacing between adjacent markers is equivalent to having 1750/25 = 70 markers. If the linkage map is smaller because of fewer polymorphic markers between the parents, the  $N_{\rm M}$ equivalent to a 25-cM spacing would be even smaller. On the other hand, the  $N_{\rm M}$  needed would be higher for recombinant inbreds, which would have undergone several meiotic events during their development.

## **Applications in Plant Breeding**

Our results for 969 maize populations show that predicting  $r_{\rm MG}$  is difficult. The observed  $r_{\rm MG}$  values were centered around the expected  $r_{\rm MG}$  when recombination between a QTL and marker was accounted for (Eq. [2]), but the spread of the observed  $r_{\rm MG}$  around the expected  $r_{\rm MG}$  was large. Breeders should also be aware that  $r_{\rm MG}$  as well as the ability to predict  $r_{\rm MG}$  differ among traits: grain yield tended to have lower  $r_{\rm MG}$  and lower predictability of  $r_{\rm MG}$  compared with moisture and test weight.

Our results suggest that  $r_{\rm MG}$  is best predicted from both  $r^2(Nh^2)^{1/2}$  and  $E(r_{\rm MG\_r2})$  from Eq. [2]. The correlations with  $r_{\rm MG}$  were equal for  $r^2(Nh^2)^{1/2}$  and for  $E(r_{\rm MG\_r2})$ , but the former cannot predict the actual value of  $r_{\rm MG}$ . As

a rule of thumb, we recommend  $r^2(Nh^2)^{1/2}$  to be at least 8. Such a rule of thumb would lead to about 90% of the  $r_{\rm MG}$  values exceeding 0.50. When  $r^2(Nh^2)^{1/2}$  is between 5 and 6, about 50% or more of the  $r_{\rm MG}$  values would exceed 0.50 for most traits. These rules of thumb apply to using a subset of a biparental cross to predict the performance of a remaining, unphenotyped subset of the same biparental cross or for recurrent genomewide selection within the same biparental cross (Combs and Bernardo, 2013b; Massman et al., 2013). Other rules of thumb need to be developed for other types of training populations (e.g., pooled biparental crosses; Jacobson et al., 2014). Also, a marker density of 70 SNP loci seems sufficient for  $F_2$  lines or DH lines developed from an elite biparental cross.

We offer a final thought on predicting  $r_{MG}$ : we are unable to precisely predict  $r_{\rm MG}$  for each population in the same way that breeders are unable to precisely predict  $h^2$ , which measures the effectiveness of phenotypic selection. While we know how increasing the number of replications and environments increases the entry-mean  $h^2$ , breeders do not devote time in trying to predict  $h^2$ . Instead, a breeder designs a yield trial on the basis of knowledge of how the traits vary in different environments, selects lines often without regard for  $h^2$  in the trial, accepts that the outcome of selection decisions will be poor if  $h^2$  is low, but is confident that selection progress can be made when averaged across different populations. We believe that, likewise, breeders should use information of how different factors affect  $r_{MG}$ , design a genomewide selection experiment accordingly, be prepared that the outcome of genomewide-selection decision will be poor if  $r_{MG}$ happens to be low in a particular test population, but be confident that routine application of genomewide selection across a breeding program will, on average, lead to positive gains. The results from the 969 maize biparental populations in this study should serve as a useful guide in the design of genomewide selection programs.

### Supplemental Information Available

Supplemental information is included with this article.

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